

CS-117: Assignment 1

**The Numerian Quest**

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# Number Systems:

## Introduction:

Number systems are just a way to for expressing numbers in a consistent and determinable manner using a set amount of symbols.

When “N” numbers of unique symbols are used we call the number system a “Base N” number system.

## Commonly used systems:

### Decimal (Base 10):

We use this number system most commonly in our life, we have intuition for this number system.

In this number system we use 10 symbols:

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

We use this number system for general communication.

For General Conversion from we convert from and then from .

### Binary (Base 2):

This number system is used by computer. As computer treats electrical signal as either on (1) or off (0) this number system is extremely important because it allows humans to perform binary arithmetic operations inand convert the output to .

In this number system we use 2 symbols:

|  |  |
| --- | --- |
| 0 | 1 |

Conversion from binary to decimal and vice versa are explained in Special Conversion Section.

### Octal (Base 8):

This number system was created to visualize computer bytes in a more readable form. This system was used as a shorthand representation of binary numbers because each group of three binary digits (bits) can be represented by one octal digit. This number system is used by UNIX operating systems today to represent file permissions.

In this number system we use 8 symbols:

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |

Conversion from octal to decimal and vice versa are explained in Special Conversion Section.

### Hexadecimal (Base 16):

This number system is the modern standard to represent binary number. In hexadecimal instead of 3 bits to represent one octal number, a hexadecimal number can represent a group of 4 bits. This is very useful as computer operates on a byte (a group of 8 bits) of data at a time, so using 2 hexadecimal digits we can represent 1 complete byte. This number system is most used to represent computer memory or memory related things.

In this number system we use 16 symbols:

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| A\* | B\* | C\* | D\* | E\* | F\* |  |  |  |  |

\* Can be upper or lower case

Conversion from hexadecimal to decimal and vice versa are explained in Special Conversion Section.

# Conversion:

## General Conversion:

To convert from one arbitrary base N to another arbitrary base M:

1. Convert from Base N to Decimal

Suppose Base N number,

Then

Here:

* number of unique symbols in the base
* the value of the digit
* index from left

1. Convert from Decimal to Base M

Apply Modulo operator until remainder is 0 or less than M, store them is a list as .

Then

## Special Conversion:

### Binary to Decimal:

Binary numbers can be represented in decimal form as follows:

1. Suppose a binary number .
2. To convert this number into decimal form we:
3. To generalize, we add the following for all digits:

### Decimal to Binary:

Divide by 2 repeatedly and note the remainders. Suppose for number 18:

|  |  |  |  |
| --- | --- | --- | --- |
| 2 | 18 | , | 0 |
| 2 | 9 | , | 1 |
| 2 | 4 | , | 0 |
| 2 | 2 | , | 0 |
|  | 1 |  |  |

Since we need to write remainders in reverse order,

### Octal to Decimal:

Same as general, we multiply by .

Example:

### Decimal to Octal:

1. First convert from decimal to binary
   1. Suppose , then in binary
2. Separate into groups of three.
3. Represent each group as an octal number.
   1. Groups are and , in octal form and respectively.
4. Combine the numbers to get final answer.
   1. This

### Hexadecimal to Decimal:

Same as general, we multiply by .

Example:

### Decimal to Hexadecimal:

1. First convert from decimal to binary
   1. Suppose , then in binary
2. Separate into groups of four.
3. Represent each group as a hexadecimal number.
   1. Groups are and , in hexadecimal form and respectively.
4. Combine the numbers to get final answer.
   1. This

# Custom Number System:

For the assignment I used a number system of 32, with the following symbols.

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| a | b | c | d | e | f | g | h | i | j |
| k | l | m | n | o | p | q | r | s | t |
| u | v |  |  |  |  |  |  |  |  |

### Custom to Decimal:

Same as general, we multiply by .

Example:

### Decimal to Custom:

Same as general, we divide by , and note remainders, remainders in reverse are our numbers.

Example:

|  |  |  |  |
| --- | --- | --- | --- |
| 32 | 788 | , | 20 |
| 32 | 24 | , |  |
|  |  |  |  |

These remainders are mapped as, and

Thus

# Links:

**Email:** [mmujtaba.bese25seecs@seecs.edu.pk](mailto:mmujtaba.bese25seecs@seecs.edu.pk)

**Github Repository Link:** <https://github.com/mmujtaba25/cs-117-assignment-1>